

Integrals to know

$$\int dx = x + C \quad \int e^x dx = e^x + C$$

$$\int a^x dx = \frac{a^x}{\ln(a)} + C \quad \int x^n dx = \frac{x^{n+1}}{n+1} + C$$

$$\int e^{ax} dx = \frac{1}{a} e^{ax} + C \quad \int \frac{1}{x} dx = \ln|x| + C$$

$$\int \ln(x) dx = x \ln(x) - x + C$$

$$\int \sin(x) dx = -\cos(x) + C \quad \int \sin(ax) dx = -\frac{1}{a} \cos(ax) + C$$

$$\int \cos(x) dx = \sin(x) + C \quad \int \cos(ax) dx = \frac{1}{a} \sin(ax) + C$$

$$\int \tan(x) dx = -\ln|\cos(x)| + C \quad \int \tan(ax) dx = -\frac{1}{a} \ln|\cos(ax)| + C$$

$$\int \cot(x) dx = \ln|\sin(x)| + C \quad \int \cot(ax) dx = \frac{1}{a} \ln|\sin(ax)| + C$$

$$\int \sec^2(x) dx = \tan(x) + C \quad \int \sec^2(ax) dx = \frac{1}{a} \tan(ax) + C$$

$$\int \csc^2(x) dx = -\cot(x) + C \quad \int \csc^2(ax) dx = -\frac{1}{a} \cot(ax) + C$$

$$\int \sec(x) \tan(x) dx = \sec(x) + C \quad \int \csc(x) \cot(x) dx = -\csc(x) + C$$

$$\int \frac{1}{a^2 + x^2} dx = \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) + C \quad \int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1}\left(\frac{x}{a}\right) + C$$

Trig Identities to know

$$\tan \theta = \frac{\sin \theta}{\cos \theta} \quad \cot \theta = \frac{\cos \theta}{\sin \theta} = \frac{1}{\tan \theta}$$

$$\sec \theta = \frac{1}{\cos \theta} \quad \csc \theta = \frac{1}{\sin \theta}$$

Note that $\sec \theta$ is not the same as $\cos^{-1} \theta$ (Aka, arccos). Same for the others too.

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$1 + \tan^2 \theta = \sec^2 \theta$$

$$\cot^2 \theta + 1 = \csc^2 \theta$$

$$\sin(2\theta) = 2 \sin \theta \cos \theta$$

$$\cos(2\theta) = 2 \cos^2(\theta) - 1 = \cos^2 \theta - \sin^2 \theta = 1 - 2 \sin^2 \theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

$$\tan(2\theta) = \frac{2 \tan \theta}{1 - \tan^2 \theta}$$